

EXTENDED MASS RELATION FOR SEVEN FUNDAMENTAL MASSES AND NEW EVIDENCE OF LARGE NUMBERS HYPOTHESIS

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ABSTRACT

A previously derived mass relation has been extended to seven equidistant fundamental masses covering an extremely large mass range from $\sim 10^{-69}$ to $\sim 10^{53}$ kg. Six of these masses are successfully identified as mass of the observable universe, Eddington mass limit of the most massive stars, mass of hypothetical quantum "Gravity Atom" whose gravitational potential is equal to electrostatic potential e^2/S , Planck mass, Hubble mass and mass dimension constant relating masses of stable particles with coupling constants of fundamental interactions. The seventh mass, $\sim 10^{-48}$ kg remains unidentified and could be considered as a prediction of the suggested mass relation for an unknown fundamental mass, potentially a yet unobserved light particle. First triad of these masses describes macro objects, the other three masses belong to particle physics masses and the Planck mass appears intermediate in relation to these two groups. Additionally, new evidences of Dirac Large Numbers Hypothesis (LNH) have been found in the form of series of ratios relating cosmological parameters and quantum properties of space-time. A very large number on the order of 5×10^{60} connects mass, density, age and size of the observable universe with Planck mass, density, time and length, respectively.

Keywords: Mass Relation, Fundamental Masses, Dirac Large Numbers Hypothesis, Newtonian Constant of Gravitation

1. INTRODUCTION

Discovery of theoretical or empirical mass relations for the many various particles is a great challenge for the recent high-energy physics and astrophysics and derivation of mass relations covering a very large range of particle masses is most desirable. Known are a few formulas connecting the masses of particles having similar properties, one such, is Hadron's multiplets (octets and decuplets of particles having close masses).

Though imprecise, one of the first attempts to empirically derive 'Balmer's law' for several particles has been attempted from (Nambu, 1952), wherein,

$m_n \sim 137 n m_e$ is the mass of the n th particle, m_e is mass of the electron and n is an integer or half-odd. Based on SU(3) symmetry, the Gell-Mann-Okubo mass formula (Gell-Mann, 1961; Okubo, 1962) has been derived for baryon decuplet: $m_\Delta - m_\Sigma = m_\Sigma - m_\Xi = m_\Xi - m_\Omega$, where m_Δ , m_Σ , m_Ξ and m_Ω are the masses of respective hyperons. This formula successfully predicted the mass for the then undiscovered Ω^- hyperon. The mass relations of (Georgi and Jarlskog, 1979) ensue from the SO(10) model and relate masses of charged leptons (e , μ and τ) and down-type quark (d , s and b) $m_e = m_d/3$, $m_\mu = 3m_s$ and $m_\tau = m_b$. However, these mass relations yield results that deviate significantly as compared to experimental data. It is postulated in (Barut, 1979) that a quantized magnetic

self-energy of magnitude $3m_e n^4 / (2\alpha)$ be added to the rest mass of a lepton to get the next heavy lepton in the chain e, μ, τ, \dots , with $n = 1$ for μ , $n = 2$ for τ . Here, α is the fine structure constant, $m_e \approx 0.511$ MeV is the mass of the electron and n is a new quantum number. Thus it was predicted $M_\tau = 1786.08$ MeV and for the next lepton $M_\delta = 10293.7$ MeV. Koide (1993) has pointed out that the mass relation $m_e + m_\mu + m_\tau = (2/3)(\sqrt{m_e} + \sqrt{m_\mu} + \sqrt{m_\tau})^2$ is consistent with the measurements of the tau lepton mass. Found in (Valev, 2008) is a simple mass relation $m_i = m_e \alpha_i(0) / \alpha$ connecting masses of stable particles (proton, electron, neutrino ν_e and graviton) with coupling constants $\alpha_i(0)$ of the four interactions and $i = 1, 2, 3, 4$. This mass relation covers an extremely wide range of values, exceeding 40 orders of magnitude and predicts a graviton mass on the order of 10^{-69} kg.

Found in (Forsythe, 2009) is the derived mass relation:

$$M_n = m_e (\sqrt{3\pi} N)^n \alpha^{2n-1} \quad (1)$$

where, $N \sim 6.02 \times 10^{23}$ is a large pure number and $n = 1, 2, 3, 4$.

This mass formula produces four equidistant masses covering a large range of 61 orders of magnitude. Mass $M_1 \sim 2.18 \times 10^{-8}$ kg is apparent Planck mass $m_p = (hc / G)^{1/2}$, $M_2 \sim 3.80 \times 10^{12}$ kg is the apparent mass of a hypothetical quantum "Gravity Atom" whose gravitational potential is equal to electrostatic potential e^2 / S , $M_3 \sim 6.62 \times 10^{32}$ kg has not been identified and $M_4 \sim 1.16 \times 10^{53}$ kg is the assumed proper mass of the observable universe. Now, in the present paper, we extend mass relation (1) to produce seven equidistant fundamental masses covering extremely large mass range of 122 powers of magnitude.

Dirac (1937) noticed that the ratio of the age of the universe H^{-1} , the inverse of the Hubble parameter and the atomic unit of time, $\tau = e^2 / m_e c^3 \approx 10^{-23}$ s, is a large number $N_D \sim 4.64 \times 10^{40}$, where e is electron charge and c is speed of light in vacuum. Additionally, the ratio of mass of the observable universe M_u and nucleon mass is of the order of N_D^2 and the ratio of electrostatic e^2 / r^2 and gravitational forces Gm_e / r^2 between proton and electron in a hydrogen atom is 2.27×10^{39} , where G is the Newtonian constant of gravitation and m_e and m_p are electron and proton masses respectively. These "coincidences" hint at a possible connection between macro and microphysical world known as Dirac Large Numbers Hypothesis (LNH). Many other interesting ratios have been found approximately relating some astrophysical (cosmological) parameters and microscopic

properties of the matter. For example Jordan (1947) noted that the mass ratio for a typical star and an electron is of the order of 10^{60} . Narlikar (1977) shows that the ratio of the observable universe radius, cH^{-1} and the classical electron radius, $e^2 / m_e c^2$ is exactly equal to N_D . Additionally, the ratio of the electron mass and Hubble mass parameter hH / c^2 is 3.39×10^{38} (Cetto *et al.*, 1986). Here $h = h / (2\pi)$ is the reduced Planck constant and H is the Hubble constant. Peacock (1999) points out that the ratio of Hubble distance cH^{-1} and Planck length l_p is on the order of 10^{60} . Besides, the ratio of Planck density ρ_p and recent critical density of the universe ρ_c is found to be on the order of 10^{121} (Andreev and Komberg, 2000). Further, the ratio of observable universe mass and Planck mass is on the order of 10^{61} (Shemi-Zadeh, 2002). These ratios between astrophysical parameters and microscopic properties of matter result mostly in large numbers that roughly agree with order of magnitude accuracy. Valev (2012) derived a series of ratios relating cosmological parameters (mass M , density $\bar{\rho} = \rho_c$, age H^{-1} and size cH^{-1} of the observable universe) and Planck (mass m_p , density ρ_p , time t_p and length l_p) respectively, resulting in a very large number N_V , wherein m_p is defined as the mass whose reduced Compton wavelength and Schwarzschild radius r_s are equal, l_p is identical with r_s and ρ_p is defined as the density of a sphere having mass m_p and radius l_p :

$$\begin{aligned} \sqrt{\frac{M}{m_H}} &= \frac{M}{m_p} = \frac{m_p}{m_H} = \frac{cH^{-1}}{l_p} = \frac{H^{-1}}{t_p} = \sqrt{\frac{\rho_p}{\bar{\rho}}} = \frac{n!}{r!(n-r)!} \\ \sqrt{\frac{c^5}{2GhH^2}} &= N_V \approx 5.73 \times 10^{60} \end{aligned} \quad (2)$$

These ratios exactly connect cosmological and quantum parameters of space-time and appear to be a precise formulation and proof of LNH. In this study, we have found new evidences in support of LNH connecting cosmological parameters and microscopic properties of matter.

2. EXTENDED MASS RELATION FOR SEVEN FUNDAMENTAL MASSES

2.1. Review of Mass Relation Concerning Four Fundamental Masses

In the previous paper (Forsythe, 2009), Newton's law of universal gravitation is derived, based on postulated

mass/energy resonance waves, wherein the apparent Newtonian constant of gravitation factors as:

$$G = \frac{c^3 \lambda_\phi^2}{6\pi h N^2} = \frac{hc}{6\pi m_\phi^2 N^2} = \frac{\hbar c}{3(\pi \alpha m_e N)^2} \cong 6.663 \times 10^{-11} m^3 kg^{-1} s^{-2} \quad (3)$$

where, m_e is electron rest mass, λ_ϕ the resonance wavelength, m_ϕ the associated particle mass and N is a large pure number, curiously comparably with N_A , the 2006 recommended numerical value of Avogadro's number and in terms of the fine structure constant α and π , is shown to be given by Equation 4:

$$N = \sqrt{8/3} (4\pi\alpha^5)^2 \cong 6.022 \times 10^{23} \quad (4)$$

The Planck mass by convention is $m_p = (\hbar c / G)^{1/2}$ (Planck, 1959). Therefore, it follows from Equation 3 that the apparent Planck mass is given by:

$$m_p = \sqrt{3\pi\alpha} m_e N = m_e (\sqrt{3\pi} N) \alpha \cong 2.18 \times 10^{-8} kg \quad (5)$$

Additionally shown is that the resonance wavelength is equal to twice the first Bohr orbit thus leading directly to:

$$m_\phi = \pi\alpha m_e \cong 2.09 \times 10^{-32} kg \quad (6)$$

It is known that the fine structure constant, the coupling constant of electromagnetic interaction, i.e., a measure of its strength, is determined by the formula $\alpha = e^2 / (\hbar c)$. Taking into consideration this formula, we find from Equation 3 that:

$$G = \frac{e^2}{3\pi^2 \alpha^3 m_e^2 N^2} \quad (7)$$

In section II of paper (Forsythe, 2009), a hypothetical quantum "Gravity Atom" has been proposed, comprised of an electrically neutral central mass M_G orbited by an electrically neutral particle having electron mass m_e such that the gravitational potential $GM_G m_e / S$ is equal to an electrostatic potential e^2 / S and S , the orbital radius, is a Bohr orbit. Thus, $GM_G m_e = e^2$, that in conjunction with Equation 7 results in:

$$M_G = 3\pi^2 \alpha^3 m_e N^2 = m_e (\sqrt{3\pi} N)^2 \alpha^3 \cong 3.80 \times 10^{12} kg \quad (8)$$

It is also of interest to note that this is the mass for which the Schwarzschild radius is equal to twice the classical electron radius.

Noted in (Forsythe, 2009) is that examination of Equation 5 and 8 reveals the masses m_p and M_G are members of the series suggested by Equation 1, that in conjunction with Equation 6 can also be expressed as $M_n = \pi^{n-1} \alpha^{2n-2} m_\phi (\sqrt{3} N)^n$, where n is the placement within the series. Employing Equation 1 and beginning at $n = 1$, it is found that:

$$M_1 = m_e (\sqrt{3\pi} N) \alpha \cong 2.18 \times 10^{-8} kg \quad (9)$$

$$M_2 = m_e (\sqrt{3\pi} N)^2 \alpha^3 \cong 3.80 \times 10^{12} kg \quad (10)$$

$$M_3 = m_e (\sqrt{3\pi} N)^3 \alpha^5 \cong 6.63 \times 10^{32} kg \quad (11)$$

$$M_4 = m_e (\sqrt{3\pi} N)^4 \alpha^7 \cong 1.16 \times 10^{53} kg \quad (12)$$

Identified above is the physical significance attributed to masses M_1 and M_2 . Mass M_4 appears to be well within the range of estimates for the observable universe proper mass M_u (Carvalho, 1995; Valev, 2014) and as such, it represents the upper limit of the series.

2.2. Extended Mass Relation for Seven Fundamental Masses, a New Fundamental Constant K and the Hubble Parameter

Upon extending the series downwards to $n \leq 0$, we obtain:

$$M_0 = m_e (\sqrt{3\pi} N)^0 \alpha^{-1} = \frac{m_e}{\alpha} \cong 1.25 \times 10^{-28} kg \quad (13)$$

$$M_{(-1)} = m_e (\sqrt{3\pi} N)^{-1} \alpha^{-3} = \frac{m_e}{\sqrt{3\pi} N \alpha^3} \cong 7.15 \times 10^{-49} kg \quad (14)$$

$$M_{(-2)} = m_e (\sqrt{3\pi} N)^{-2} \alpha^{-5} = \frac{m_e}{3\pi^2 N^2 \alpha^5} \cong 4.10 \times 10^{-69} kg \quad (15)$$

It is found that the ratio of any two consecutive masses in the Equation 9-15 is a new fundamental constant K , wherein:

$$\frac{M_{n+1}}{M_n} = K = \sqrt{3\pi} N \alpha^2 \cong 1.77 \times 10^{20} \quad (16)$$

Therefore:

$$M_n = \frac{m_e}{\alpha} (\sqrt{3\pi N} \alpha^2)^n = \frac{m_e}{\alpha} K^n = M_0 K^n \quad (17)$$

where, $n = -2, -1, 0, \dots, 4$. We now find that:

$$\frac{2M_1}{\pi K^3} = \frac{2M_2}{\pi K^4} = \frac{2M_3}{\pi K^5} = \frac{2M_4}{\pi K^6} \cong 2.61 \times 10^{-69} \text{ kg} \quad (18)$$

The current best estimates of H_0 center around about $70 \text{ km s}^{-1} \text{ Mpc}^{-1}$. Thus, when m_H , the Hubble mass (Maor and Brustein, 2003; Gazeau and Toppan, 2010), is defined as:

$$m_H = \frac{\hbar H}{c^2} \quad (19)$$

We find from Equation 19 an approximate value for m_H of $2.66 \times 10^{-69} \text{ kg}$. This result is close to that from Equation 18. It is close enough in fact that all symbolic members of Equation 18 are assumed to express accurately the value of the Hubble mass concomitant with H . Therefore, regarding the 1st and 4th members:

$$\frac{2m_p}{\pi K^3} = m_H \quad (20)$$

And:

$$\frac{2M_u}{\pi K^6} = m_H \quad (21)$$

From which, upon elimination of K , results:

$$m_H = \frac{2m_p^2}{\pi M_u} \quad (22)$$

And the final result upon substituting the right-hand member of Equation 22 into Equation 19 for m_H and solving for H , becomes:

$$H = \frac{2c^2 m_p^2}{\pi \hbar M_u} = \frac{4c^2 m_p^2}{h M_u} \quad (23)$$

If the Hubble mass is defined as $\hbar H / c^2$, as in (Forsythe, 2009), the value for m_H would be $\sim 1.64 \times 10^{-68} \text{ kg}$, so the left-hand members of Equation 20 and 21 must then be multiplied by 2π to preserve the equalities and Equation 22 is still the final result.

As was proposed in (Forsythe, 2012), predicated upon the rate of cosmic expansion apparently transitioning from deceleration to acceleration at redshift $z \sim 0.5$ (Perlmutter *et al.*, 1999), the deceleration parameter must have passed through a zero null point at transition, as the opposing operatives of cosmic expansion reached a transient state of equilibrium. Intuitively it would seem that the Hubble parameter at that juncture H_{eq} , the tipping point between deceleration and acceleration, must be tied to the mass of the universe via means of a unique relationship that existed at that juncture, as developed through Equation 19-22, leading to Equation 23. However, it does not necessarily follow that the Hubble parameter is increasing along with the accelerating rate of cosmic expansion. Some theoretical considerations suggest that the Hubble parameter has now assumed a truly constant value in time and space. Others predict that even as the expansion accelerates, the Hubble parameter will continue to decrease asymptotically, approaching a limiting value of about $62 \text{ km s}^{-1} \text{ Mpc}^{-1}$, as the influence of the cosmological constant becomes more and more dominant over the contribution of matter after several billions of years and a several fold increase in the scale factor. It is thus reasonable to propose that H_0 , the present day Hubble parameter and H_{eq} are essentially identical. Thus Equation 24:

$$H = H_{eq} = \frac{4c^2 m_p^2}{h M_u} \cong H_0 \cong 68.63 \text{ km s}^{-1} \text{ Mpc}^{-1} \quad (24)$$

A theoretical value for H_0 of $68.66 \pm 0.1 \text{ km s}^{-1} \text{ Mpc}^{-1}$, obtained via an entirely independent approach (Bukalov, 2002), is in excellent agreement with the above.

Since by convention, the square of the Planck mass is $\hbar c / (2\pi G)$ Equation 23 can be restated as:

$$H_{eq} = \frac{2c^3}{\pi G M_u} \cong 68.63 \text{ km s}^{-1} \text{ Mpc}^{-1} \quad (25)$$

And from Equation 25, we obtain:

$$M_u = \frac{2c^3}{\pi G H_{eq}} \cong 1.16 \times 10^{53} \text{ kg} \quad (26)$$

The exact same result as that of Equation 12. Additionally, from Equation 12 and 26 another interesting relationship results Equation 27:

$$M_4 = M_u = \frac{2c^3}{\pi G H_{eq}} = m_e (\sqrt{3\pi N})^4 \alpha^7 \cong 1.16 \times 10^{53} \text{ kg} \quad (27)$$

2.3. Review of Three Fundamental Masses Obtained by Dimensional Analysis

In previous paper (Valev, 2013), three fundamental masses have been derived by dimensional analysis, namely:

$$m_1 = \frac{\hbar H}{c^2} = m_H \tag{28}$$

$$m_2 = k \frac{c^3}{GH} \equiv M_u \tag{29}$$

$$m_3 = \left(\frac{H \hbar^3}{G^2} \right)^{1/5} \equiv 1.43 \times 10^{-20} \text{ kg} \tag{30}$$

In form, Equation 26 coincides closely with Equation 29 and the two are an identity when the dimensionless parameter k , on the order of unity, is identical with $2/\pi$.

The papers (Forsythe, 2009; 2012) do not attribute any physical significance to mass $M_3 \sim 6.63 \times 10^{32}$ kg in the original n_1 through n_4 series. Recently we have identified this mass with the Eddington stellar mass limit where the outward pressure of the star's radiation balances the inward gravitational force (Vink *et al.*, 2011; Crowther *et al.*, 2012). Additionally, we have identified the mass $M_0 \sim 1.25 \times 10^{-28}$ kg as exactly coinciding with the mass dimension constant in a basic mass equation from paper (Valev, 2008) relating masses of stable particles and coupling constants of the four fundamental interactions. It is interesting that this mass is approximately a half-charged pion mass $M_0 = m_\pi / \alpha \approx 0.5 m_{\pi^\pm}$. Mass $M_{(-1)} \sim 7.15 \times 10^{-49}$ kg is presently unidentified and could feasibly be regarded as a prediction by the suggested model, Equation 9, for a fundamental, albeit as yet unobserved light particle. Finally, mass $M_{(-2)} \sim 4.10 \times 10^{-69}$ kg in the extended series is easily identifiable with the Hubble mass Equation 19 as $0.5 \pi m_H$. It is of further interest to note that the extended mass series includes seven equidistant fundamental masses covering a mass interval of 122 orders of magnitude and that masses $M_{(-2)}$, $M_{(-1)}$ and M_0 are particle physics masses, whereas the masses M_2 , M_3 and M_4 describe macro objects and the Planck mass M_1 appears intermediate in relation to these two groups. In fact, it is easily shown that the Planck mass, as given by Equation 9, is the geometric mean of the extreme masses $M_{(-2)}$ and M_4 as given by Equation 15 and 12, as is the geometric mean of masses m_1 and m_2 from Equation 28 and 29 when $k = 1$. Valev mass m_3 from Equation 30 has not

yet been identified and could be regarded as a prediction for unknown fundamental mass, most likely a yet unobserved very heavy particle.

3. NEW EVIDENCE OF DIRAC LARGE NUMBERS HYPOTHESIS

Recalling Equation 2 and the definition of terms therein, it is found that $N_V \sim 5.73 \times 10^{60}$ when the defined terms are evaluated according to: $M = c^3 / (2GH)$; $m_H = \hbar H / c^2$; $m_p = (\hbar c / 2G)^{1/2}$; $l_p = (2G\hbar / c^3)^{1/2}$; $t_p = l_p / c = (2G\hbar / c^5)^{1/2}$; $\rho_p = 3c^5 / (16\pi\hbar G^2)$; $\rho_c = 3H^2 / (8\pi G)$ is recent density of the universe equal to the critical one; H^{-1} , the age of the universe and cH^{-1} is the Hubble distance.

The Equation 2 ratios appear very important because they relate cosmological parameters and the fundamental microscopic properties of matter. The Planck units imply quantization of space-time at extremely short range. Thus, the ratios represent connection between cosmological and quantum parameters of space-time and thus appear to be a precise formulation and proof of LHN. In addition, the very large number N_V and Dirac large number N_D (Dirac, 1937) seem connected by the approximate formula Equation 31:

$$N_D \sim N_V^{2/3} = \left(\frac{c^5}{2G\hbar H^2} \right)^{2/3} \approx 3.2 \times 10^{40} \tag{31}$$

We now construct a similar series to (2) involving ratios of the same parameters producing the very large, number N_{VF} , as follows Equation 32:

$$\left(\frac{2 M_u}{\pi m_H} \right)^{1/2} = \frac{M_u}{m_p} = \frac{2 m_p}{\pi m_H} = \frac{2 c H^{-1}}{\pi l_p} = \frac{2 H^{-1}}{\pi t_p} = \tag{32}$$

$$\frac{2 \left(\frac{\rho_p}{2\rho_c} \right)^{1/2}}{\pi} = \frac{2 \left(\frac{c^5}{G\hbar H^2} \right)^{1/2}}{\pi} = N_{VF} \approx 5.31 \times 10^{60}$$

where, now:

$H = H_{eq} = 2c^3 / (\pi G M_u)$; $M_u = 2c^3 / (\pi G H)$ is apparent proper mass of the universe; $m_H = \hbar H / c^2$; $m_p = (\hbar c / 2\pi G)^{1/2}$; $l_p = (G\hbar / c^3)^{1/2}$; $t_p = l_p / c = (G\hbar / c^5)^{1/2}$; $\rho_p = 3m_p / (4\pi l_p^3) = 3c^5 / (4\pi\hbar G^2)$; $\rho_c = 3H^2 / (8\pi G)$ and G is according to Equation 3. These ratios also represent a connection between cosmological and quantum parameters of space-time

and so likewise appear to be possible new evidences of LNH. Recalling Equation 17, it is noteworthy that apparently: $N_{VF} = K^3 = (\sqrt{3}\pi N\alpha^2)^3 \cong 5.31 \times 10^{60}$ and that N_{VF} and Dirac large number N_D seem connected by the approximate formula:

$$N_D \sim N_{VF}^{2/3} = K^2 = (\sqrt{3}\pi N\alpha^2)^2 = \left(\frac{4c^5}{\pi^2 G \hbar H^2}\right)^{2/3} \cong 3.04 \times 10^{40} \quad (33)$$

Thus, by independent approaches it is apparent that we obtain very similar results, (31), (33) and (2), (32). From Equation 33, it follows that:

$$N^2 = \frac{N_{VF}^{2/3}}{3\pi^2 \alpha^4} = \frac{K^2}{3\pi^2 \alpha^4} \quad (34)$$

That upon substitution into Equation 3 for the square of N results in Equation 35:

$$G = \frac{\alpha^2 \hbar c}{m_e^2 N_{VF}^{2/3}} = \frac{\alpha^2 \hbar c}{m_e^2 K^2} \quad (35)$$

Thus, Equation 34 and 35 connect N to LNH and therefore to G through the unique and apparently new fundamental constant K , as given by Equation 16.

4. CONCLUSION

Mass relation (1) obtained in (Forsythe, 2009) has been extended from $n = -2$ to $n = 4$. The result is seven equidistant fundamental masses M_n , covering a mass interval of 122 orders of magnitude, have been obtained. Six of these masses are successfully identified, namely $M_1 \sim 2.18 \times 10^{-8}$ kg the apparent Planck mass $m_p = (\hbar c / G)^{1/2}$, that is very important in recent particle physics. The mass $M_2 \sim 3.80 \times 10^{12}$ kg is the central mass of a hypothetical quantum "Gravity Atom" whose gravitational potential $GM_G m_e / S$ is equal to electrostatic potential e^2 / S and S is a Bohr orbit radius and the mass $M_3 \sim 6.63 \times 10^{32}$ kg is of the order of the Eddington mass limit of the most massive stars. The mass $M_4 \sim 1.16 \times 10^{53}$ kg is close to the mass of the Hubble sphere and most probably appears to be mass of the observable universe. The mass $M_0 \sim 1.25 \times 10^{-28}$ kg coincides with a mass dimension constant in a basic mass equation relating masses of stable particles and coupling constants of the four interactions; approximately a half charged pion mass. The mass $M_{(-2)} \sim 4.10 \times 10^{-69}$ kg is easily identifiable

with the Hubble mass as $0.5 \pi m_H$. The mass $M_{(-1)} \sim 7.15 \times 10^{-49}$ kg remains yet unidentified and could be regarded as a prediction by the suggested mass relation for unknown fundamental mass, most likely a yet unobserved light particle. Apparently, masses $M_{(-2)}$, $M_{(-1)}$ and M_0 are particle physics masses, whereas the masses M_2 , M_3 and M_4 describe macro objects and the Planck mass M_1 appears intermediate in relation to these two groups.

Finally, new evidences of LNH have been found in the form of series of ratios relating cosmological parameters and quantum properties of space-time. In addition, the very large number $N_{VF} = K^3 = (\sqrt{3}\pi N\alpha^2)^3 \cong N_V = \sqrt{c^5 / (2G\hbar H^2)} \cong 5.31 \times 10^{60}$ connects mass, density, age and size of the observable universe with Planck mass, density, time and length respectively and K is apparently a unique and new fundamental constant.

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